

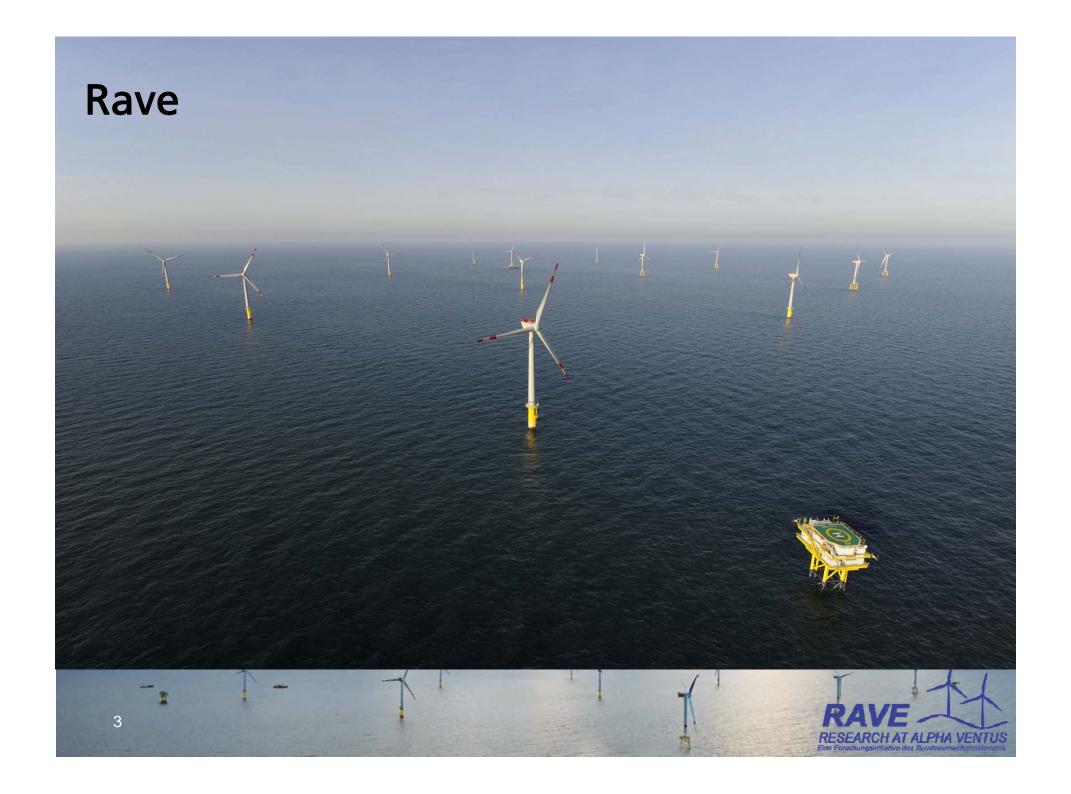






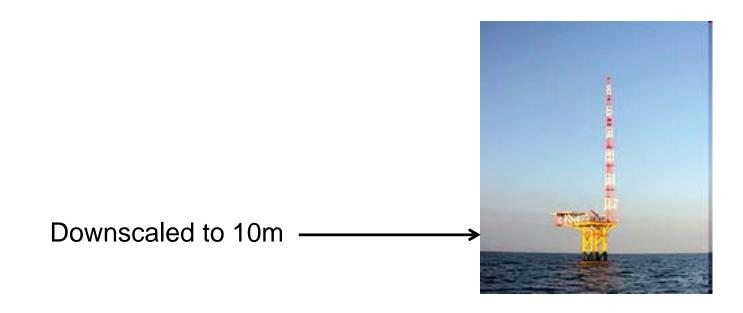
Outline

- Data
- Baseline: Assume normal errors
- Alternative 1: Variance Inflation
- Alternative 2: Gaussian Ensemble Dressing
- Conclusions









Downscaled to 10m

• Logarithmic assumption



Downscaled to 10m

• Logarithmic assumption
• Matches NWP

Forecast Input: Poor Man's Ensemble **Prediction System**













- Poor Man's Prediction Ensembles
 - 23 deterministic NWP forecasts, 20 European weather services
 - Based on four different regional models (COSMO, HIRLAM, UKMO, ALADIN)
 - Provided by DWD (German Weather Service)

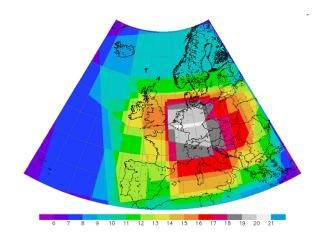
Provided by

■ Forecast horizons: 1-48 hrs



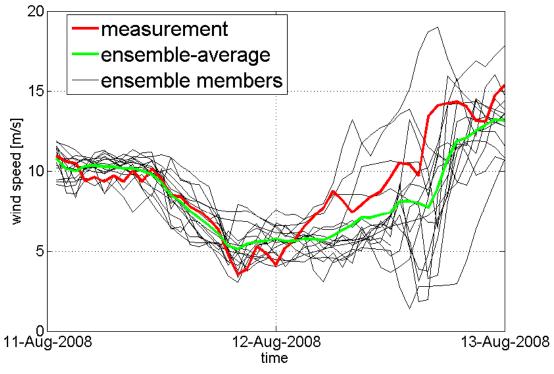


Required Spatio-Temporal Overlap → Ensemble Subset



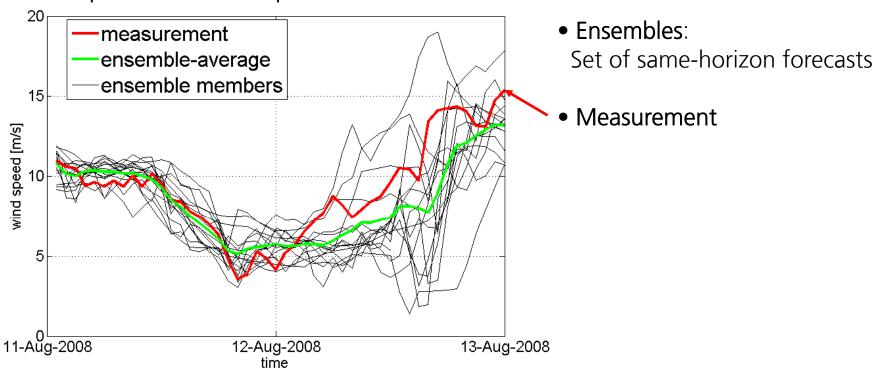
2007/2008: 12 members with sufficient data

Example of an ensemble prediction

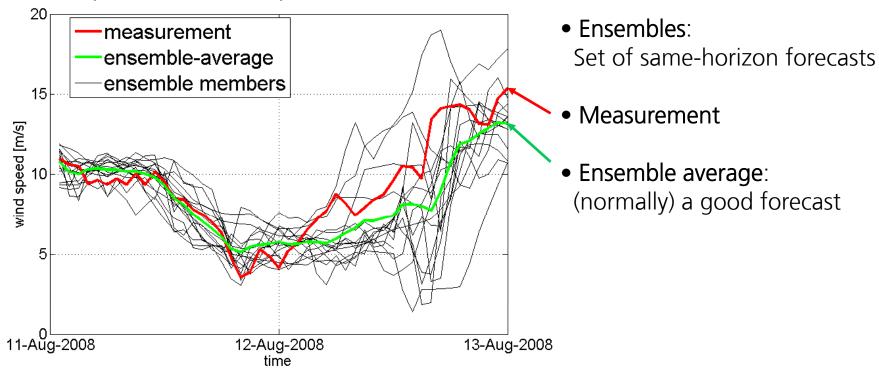


• Ensembles: Set of same-horizon forecasts

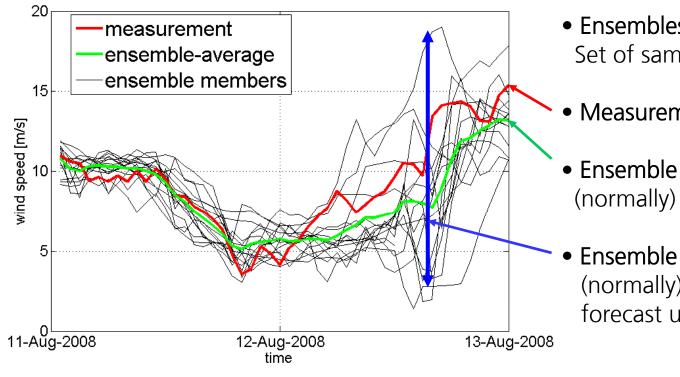
Example of an ensemble prediction



Example of an ensemble prediction



Example of an ensemble prediction



- Ensembles: Set of same-horizon forecasts
- Measurement
- Ensemble average: (normally) a good forecast
- Ensemble spread (normally) a good indicator of forecast uncertainty

Baseline System: Assume Normal Distributed Error

Assumption: Wind speed forecast error is normal distributed

$$\Delta_{ws} \sim N(\mu, \sigma^2)$$

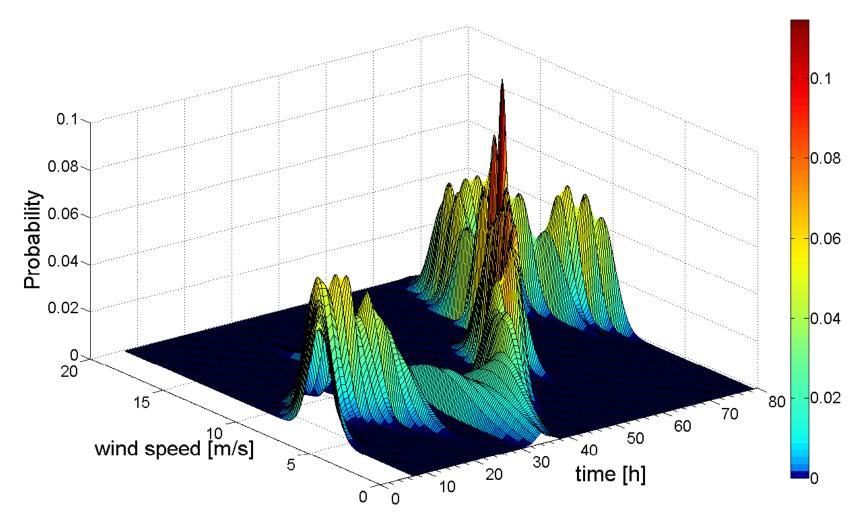
→ Probabilistic forecast at time t is based on a normal distribution

$$forecast(t) \sim N(\mu(t), \sigma^2(t))$$

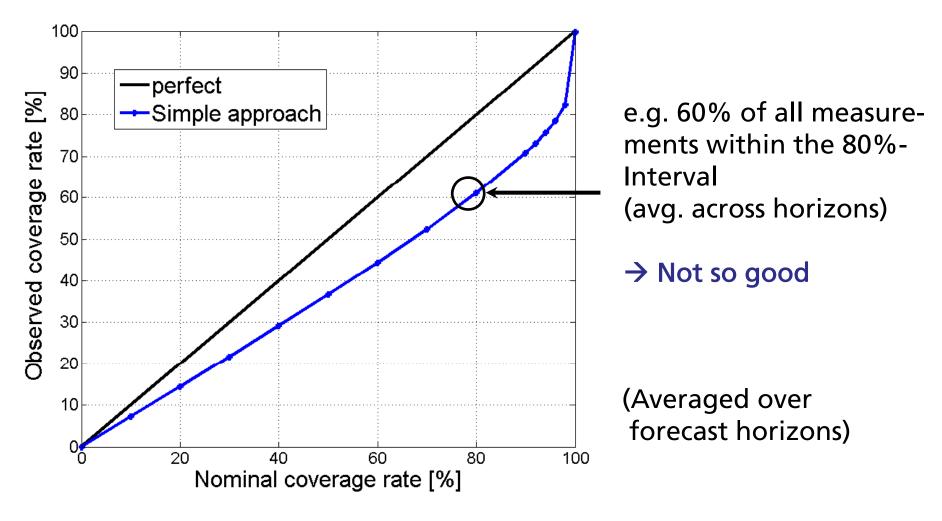
 $\mu(t)$ = ensemble average at time t

 $\sigma(t)$ = ensemble standard deviation @ t

Baseline Forecast: Normal Assumption

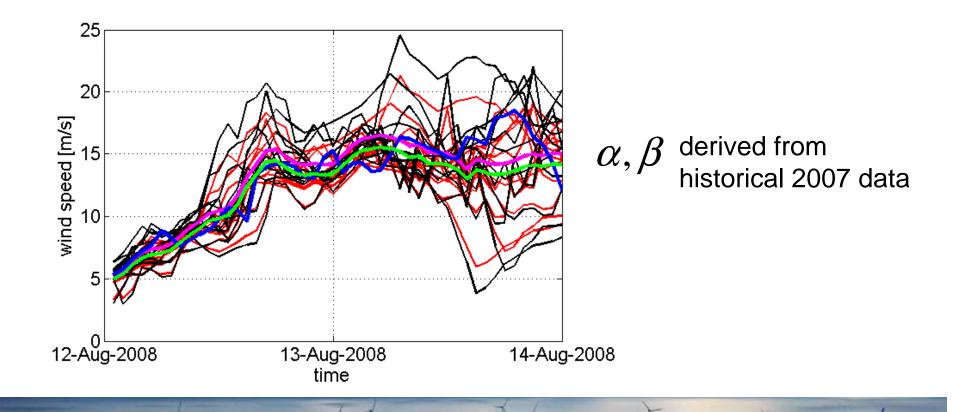


Baseline forecast: Reliability: do the distributions match?

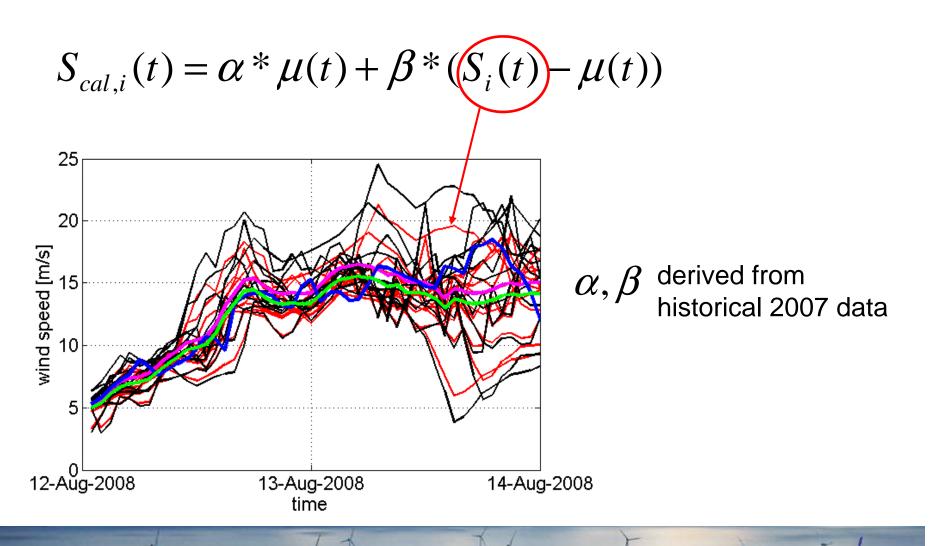


Alternative 1: Variance Inflation

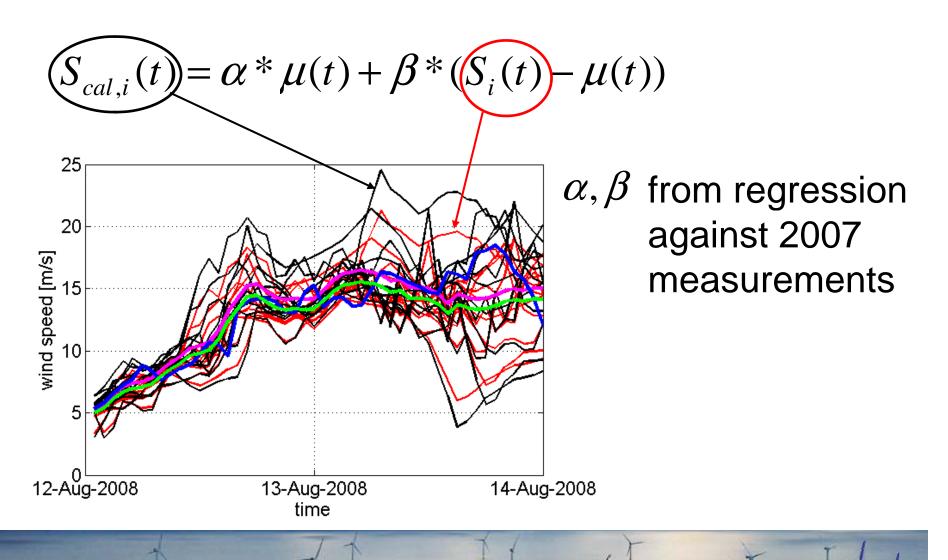
$$S_{cal,i}(t) = \alpha * \mu(t) + \beta * (S_i(t) - \mu(t))$$



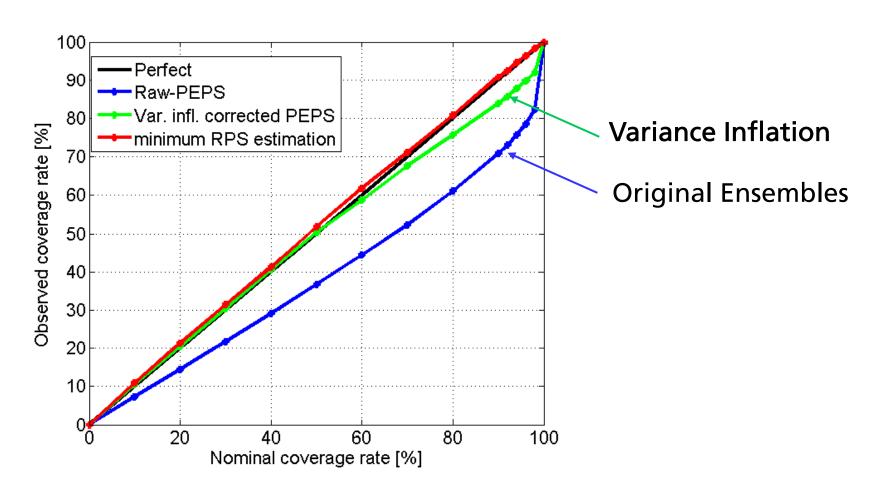
Alternative 1: Variance inflation



Alternative 1: Variance inflation



Variance Inflation: Improved Reliability



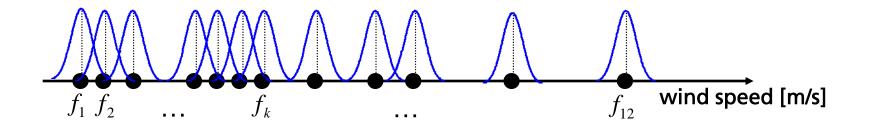


Alternative 2: Gaussian Ensemble Dressing

1.) Normal distribution around each ensemble member at time t:

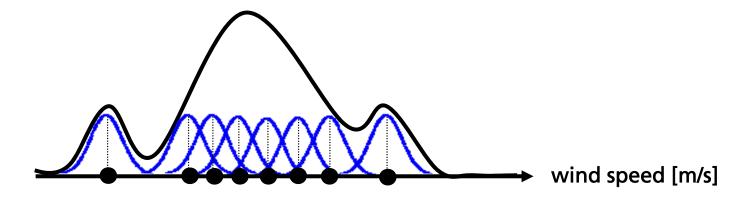
$$N_t(f_k, \sigma^2)$$
 with: f_k forecast of ensemble member k

 σ standard deviation, same for all k



2.) Weighted linear combination

$$P_{t} = \sum_{k=1}^{12} w_{k} N_{t}(f_{k}, \sigma^{2})$$
 with $\sum_{k=1}^{12} w_{k} = 1$

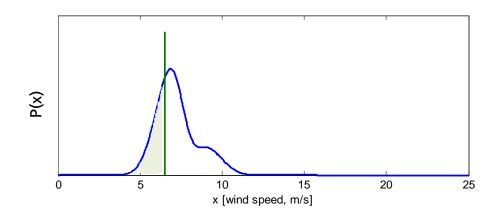


3.) Optimization of the unknown parameters: $w_1, w_2, ..., w_{12} \& \sigma$

$$P_t = \sum_{k}^{12} w_k N_t(f_k, \sigma^2)$$

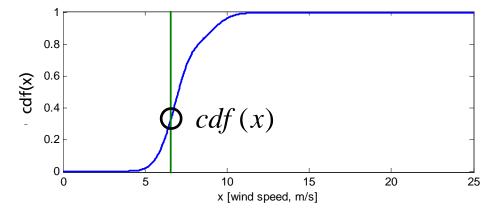
... by minimization of "Ranked Probability Score (RPS)"

Minimize the cdf difference at each time, t (over 2007 measurements)



Probability Density Function

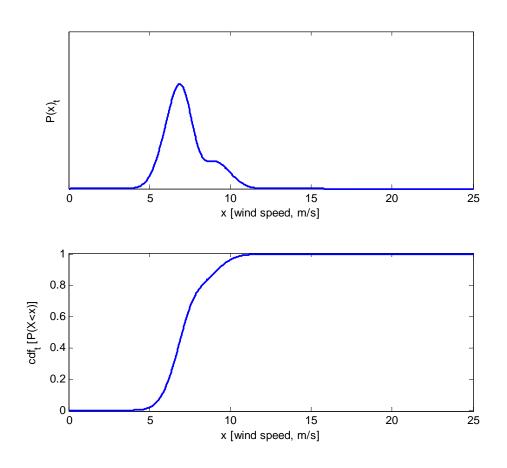
$$P(x) = prob(meas = x)$$

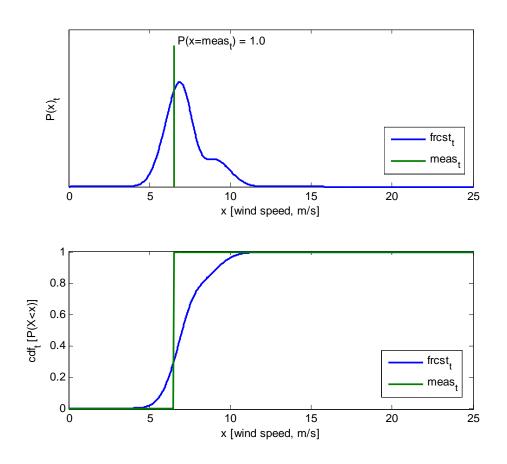


Cumulative Density Function

$$cdf(x) = prob(meas \le x)$$

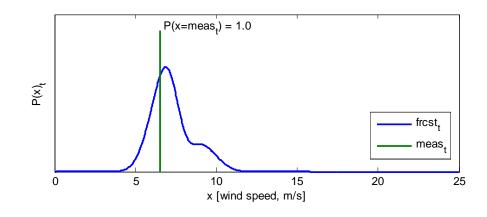




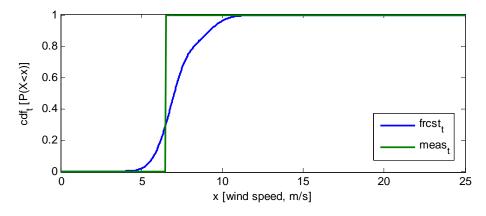


Measurement probability: 1.0



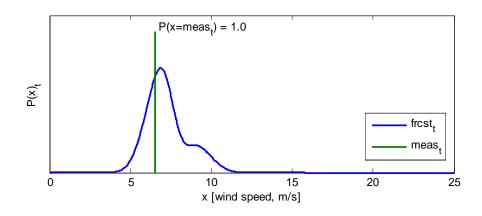


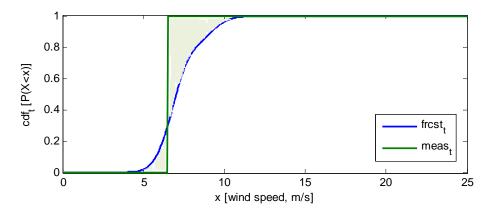
Measurement probability: 1.0



Measurement cdf: step function







→ RPS: a function of cdf error²

$$\Delta cdf(t,h) =$$

$$\int (cdf_h^{frest}(s,t) - cdf^{meas}(s,t))^2 ds$$
sewindspeed

Gaussian Ensemble Dressing: Optimization

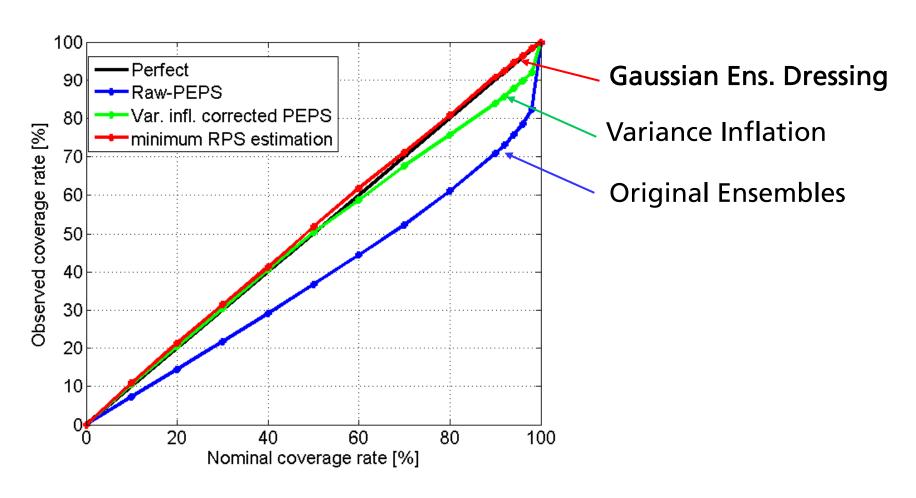
■ Optimization cost function: RPS over time, horizons

$$RPS_{\cos t} = \iint \Delta c df(t, h) dt dh$$

time, horizons

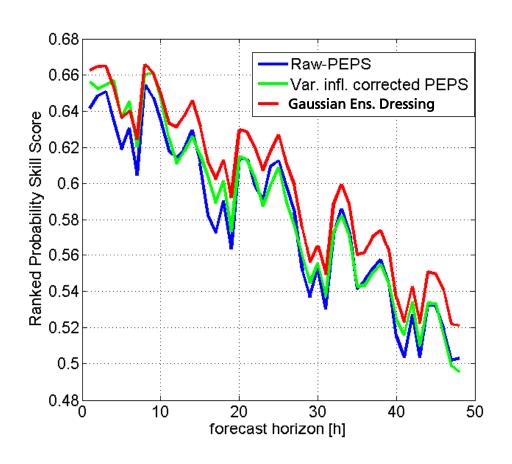
■ Optimization algorithm: Simplex

Gaussian Ensemble Dressing: Best Reliability





Gaussian Ensemble Dressing: Best skill across forecast horizons



Ranked Probability Skill Score:

$$RPSS = 1 - \frac{RPS}{RPS_{c \lim ato \log y}}$$

0 → no skill

1 → perfect skill

Gaussian Ensemble Dressing has clearly higher skill

Conclusions

- Variance scaling is an improvement, but...
- Gaussian Ensemble Dressing is best
 - highest reliability
 - highest skill
- Optimization via RPS minimization works
- Next...
 - Probabilistic power forecasts for Alpha Ventus